

Learning Actionable Insights

from scientific data and models

Jilles Vreeken | 19 May 2025

Common questions in biology



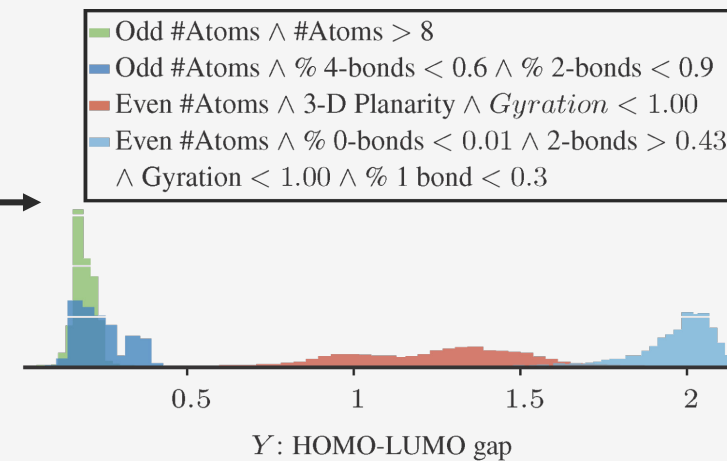
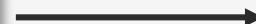
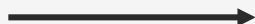
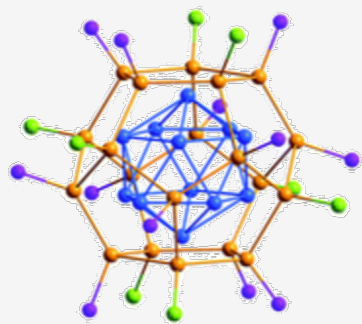
What is the difference between cancerous and benign tissue?



Common questions in physics



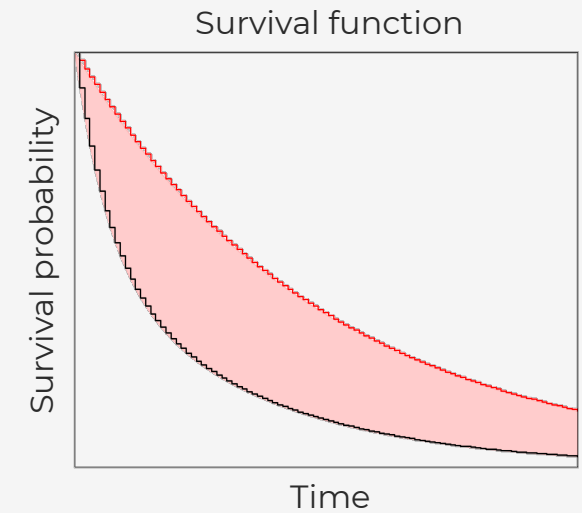
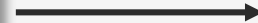
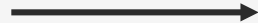
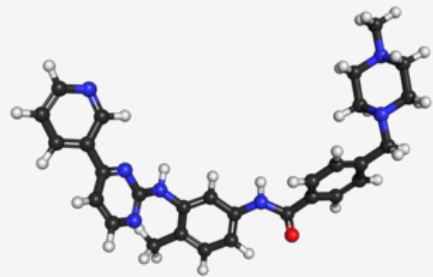
What materials have exceptional conductivity?



Common questions in medicine



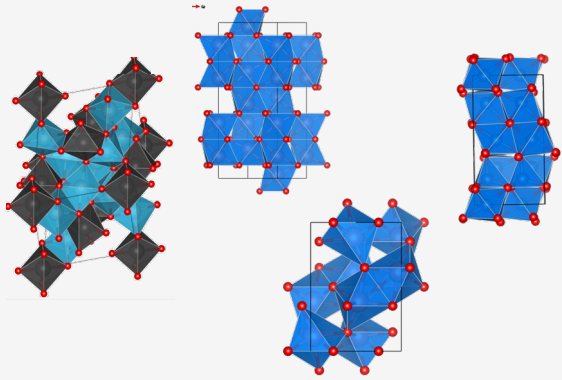
Which people do (not) benefit from a treatment?



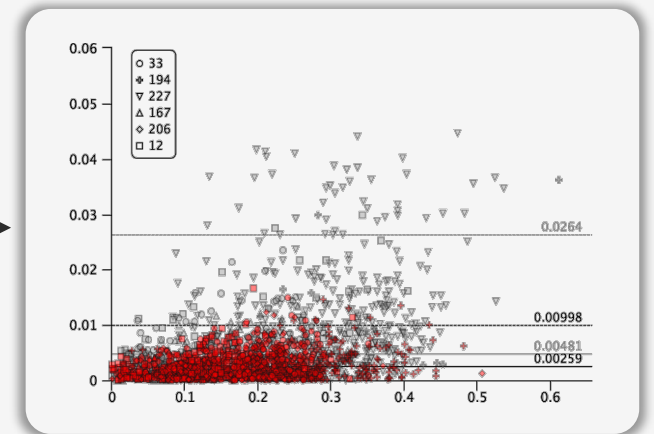
Common questions in reality



What is the domain of applicability of my ML model?



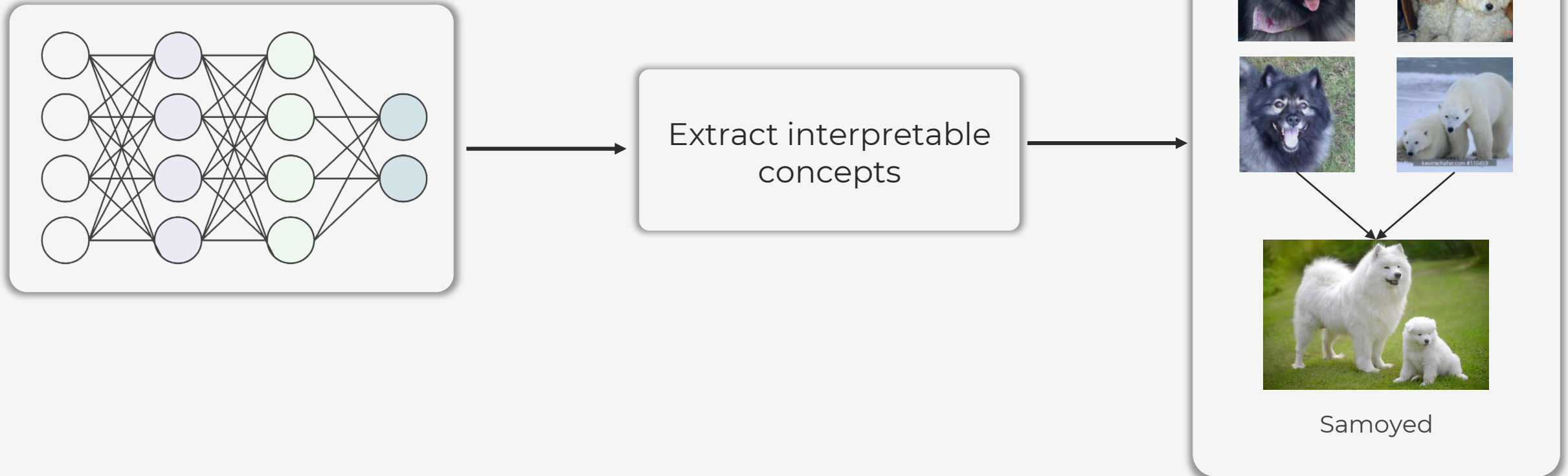
Determine conditions
on x under which $\hat{f}(x)$
is reliable



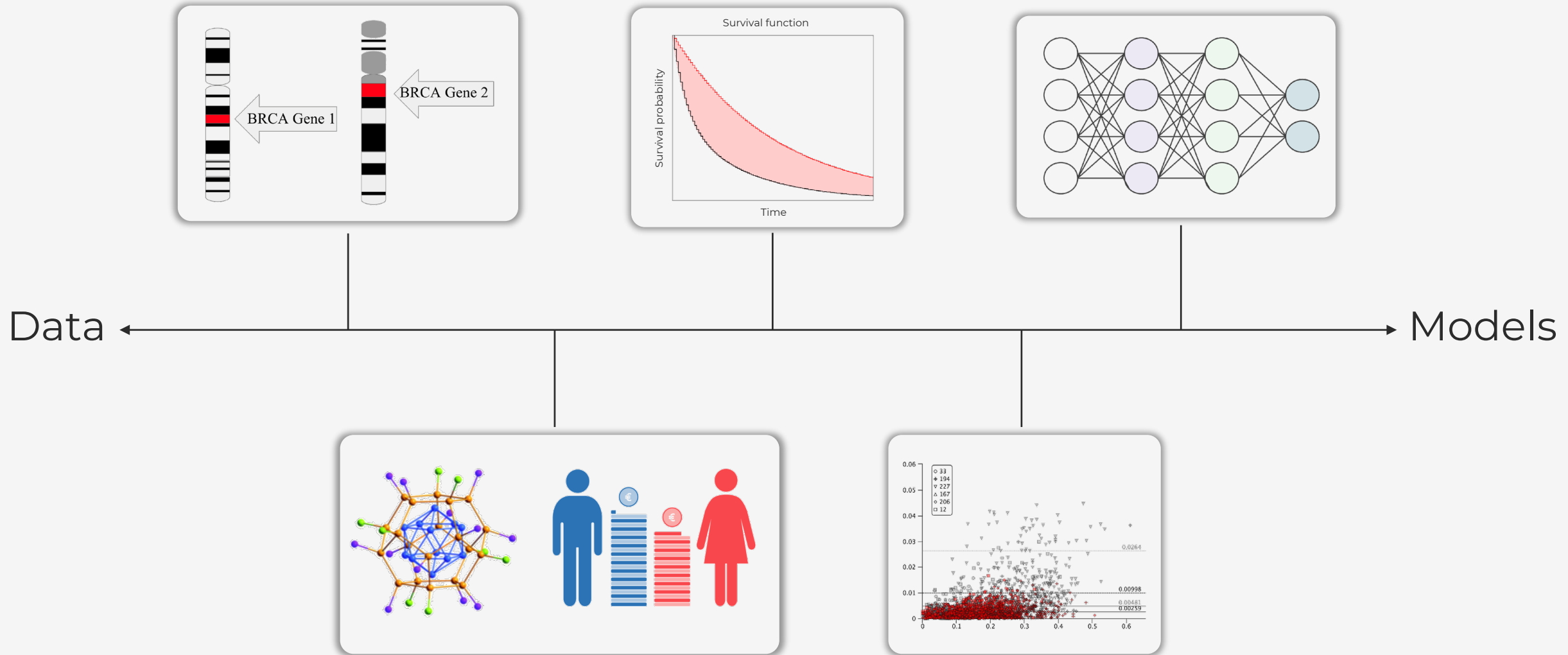
Common questions in interpretability



What internal reasoning influences predictions?



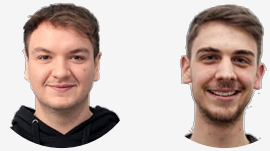
Common questions in ML



Common questions in ML

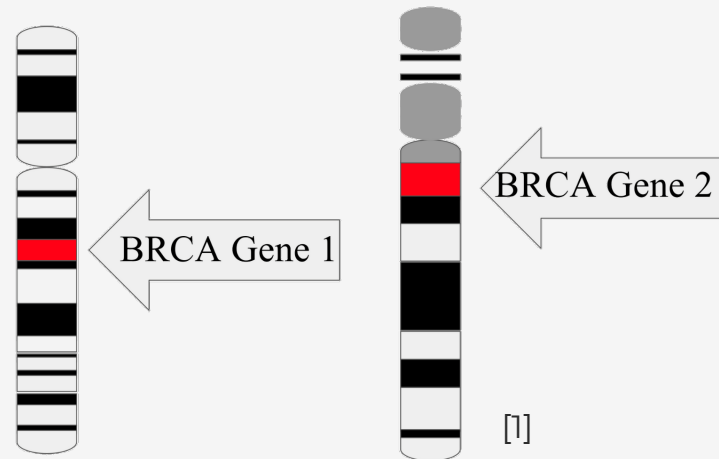


Understanding genetic data



Breast Cancer Data (BRCA)

- (Binarized) sequences of tissue samples
- Labeled with types of BRCA
- Very high-dimensional, low #samples



Goal: Find class-specific interactions of genes

Class-specific pattern:

1. Occurs more often in class k
2. Is most predictive for class k

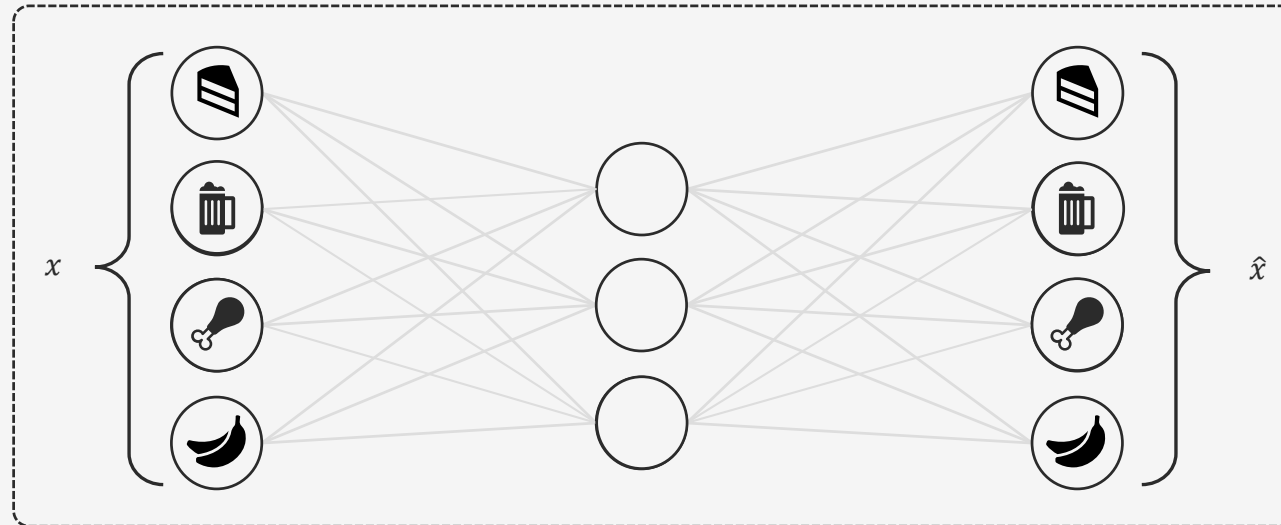
Features F						Y
						r
1	1	1	1			r
1	1	1	1	1	1	r
1	0	1	1	1	1	r
1	1	1	1	1	1	s
				1	1	s
				1	1	s
						s
						s

BiNAPS – In a nutshell



Main Idea: Compression $\rightarrow$ Patterns

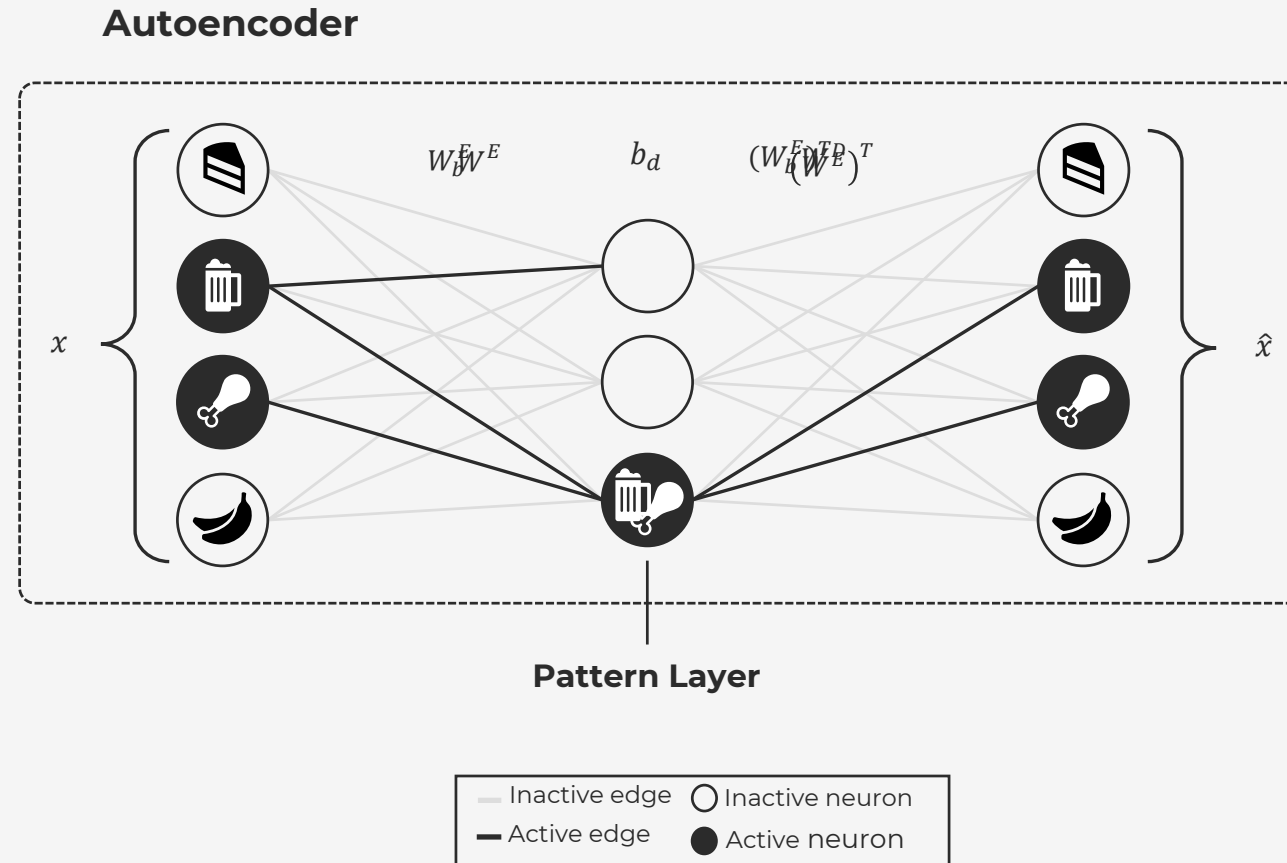
Autoencoder



BiNAPS – In a nutshell



Main Idea: Compression $\rightarrow$ Patterns

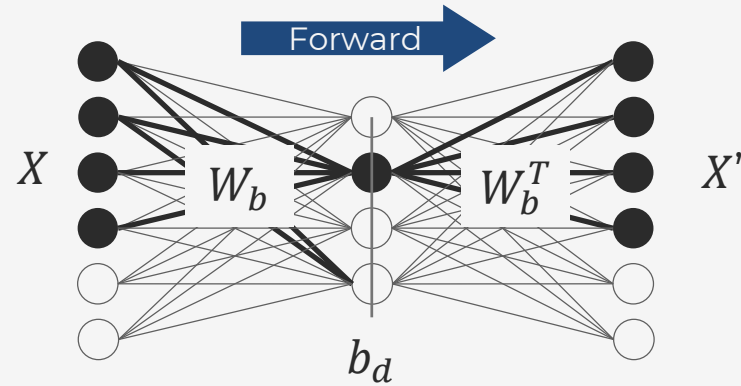


BiNAPS – In a nutshell



For $X \in D$

1. reconstruct

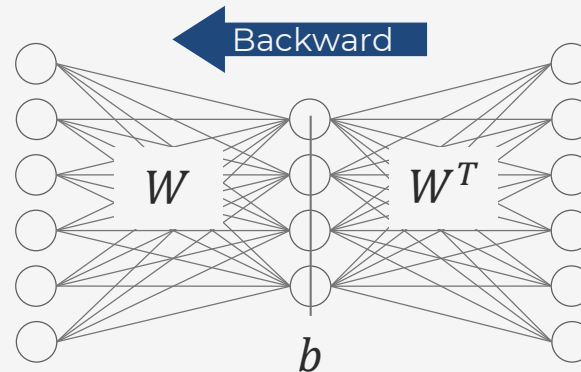


2. compute loss

$$L_{W,b}(X)$$

3. backpropagate

$$\frac{dL_{W,b}(X)}{dW} \quad \frac{dL_{W,b}(X)}{db}$$



4. Clamp W, b and get binarized W_b , discretized b_d

 PyTorch

Use ADAM for optimization

Exploring human variation.



single nucleotide polymorphisms

individuals

	1	1	0		0	0	1	1
	1	1	0		0	0	1	1
	0	1	1		1	1	0	1
	0	1	1		1	1	0	0
	1	1	0		0	0	1	1

1000 Genomes project

Measuring variations across human populations (~2500 individuals)

Here we look at single nucleotide variations in genes of autosomes (~228k variants)

Exploring human variation.



What we find:

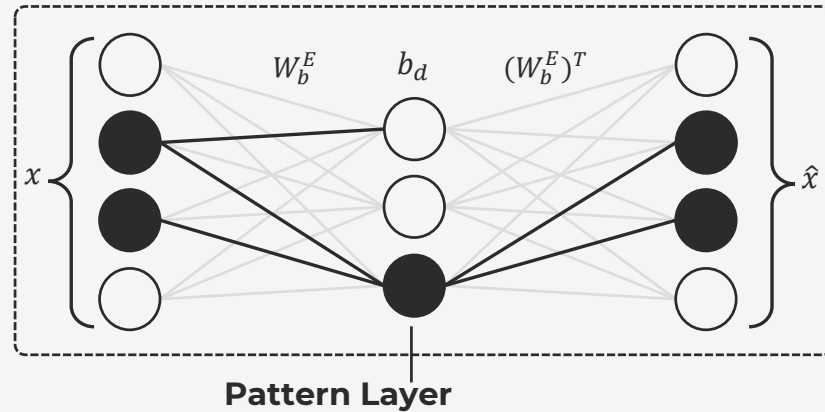
- Blocks of consecutive variation
- Patterns of alternate phasing across variants
(in some individuals pattern 0 | 1, 0 | 1, 0 | 1 in others 1 | 0, 1 | 0, 1 | 0)
- Linking to genes:
 - Pattern of developmental genes together with genes with unknown role
 - Pattern of genes crucial for the ribosomal complex
 - Pattern of variants associated with type 2 diabetes, and unknown variant

BiNAPS – In a nutshell

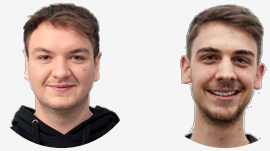


Main Idea: Compression $\rightarrow$ Patterns

Autoencoder

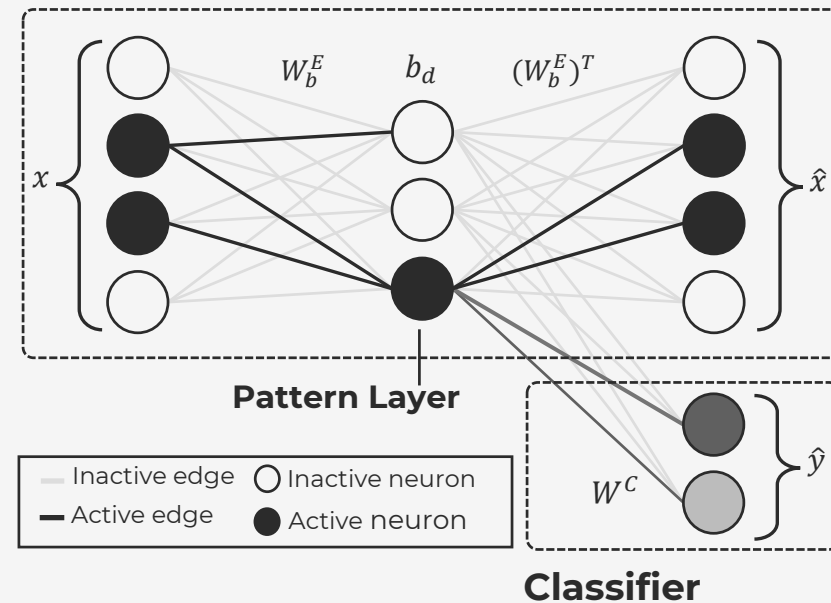


DIFFNAPS – In a nutshell



Main Idea: Compression + Classification → Class-specific pattern

Autoencoder



Forward Pass

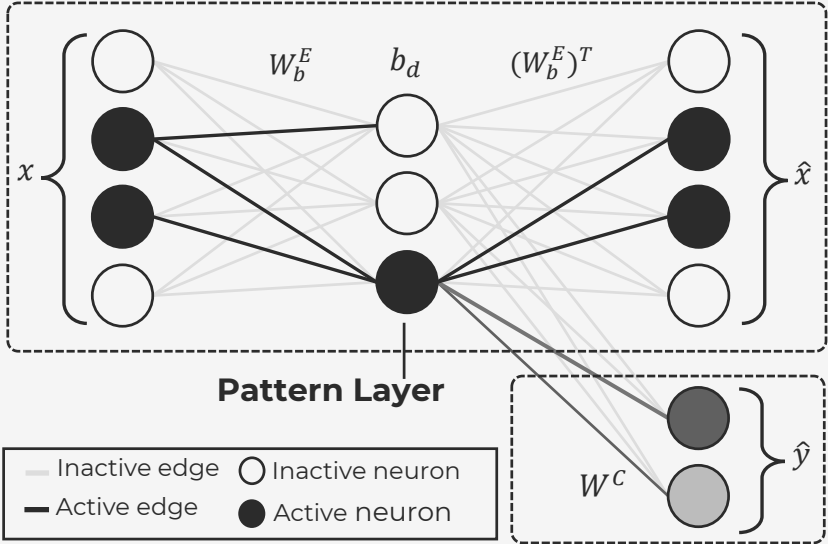
1. Binary input x
2. Binarize weight matrix W_b^E
3. Compute hidden activation z
$$z = \lambda_E(W_b^E x),$$
where λ_E is a binary activation function.
4. Compute reconstruction $\hat{x}$
$$\hat{x} = \lambda_D((W_b^E)^T z)$$
5. Compute classification $\hat{y}$
$$\hat{y} = \text{softmax}(W^C z)$$

Jointly optimize reconstruction and classification accuracy

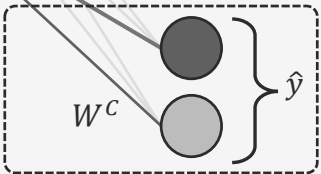
DIFFNAPS – Extract patterns



Autoencoder



Pattern Layer



Classifier

Continuous

$$W^E = \begin{bmatrix} 0.02 & \mathbf{0.87} & 0.02 & \mathbf{0.87} \\ \mathbf{0.8} & 0.01 & 0.04 & \mathbf{0.9} \\ 0.0 & \mathbf{0.99} & \mathbf{0.8} & 0.09 \end{bmatrix}$$

$$\xrightarrow{\mathcal{B}\tau_E(\cdot)}$$

Discrete

$$W_b^E = \begin{bmatrix} 0 & \mathbf{1} & 0 & \mathbf{1} \\ \mathbf{1} & 0 & 0 & \mathbf{1} \\ 0 & \mathbf{1} & \mathbf{1} & 0 \end{bmatrix}$$

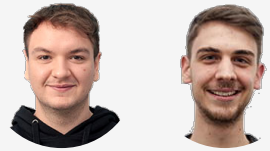
$$W^C = \begin{bmatrix} 0.07 & 0.01 & \mathbf{0.9} \\ 0.02 & \mathbf{0.9} & 0.2 \end{bmatrix}$$

$$\xrightarrow{\mathcal{B}\tau_C(\cdot)}$$

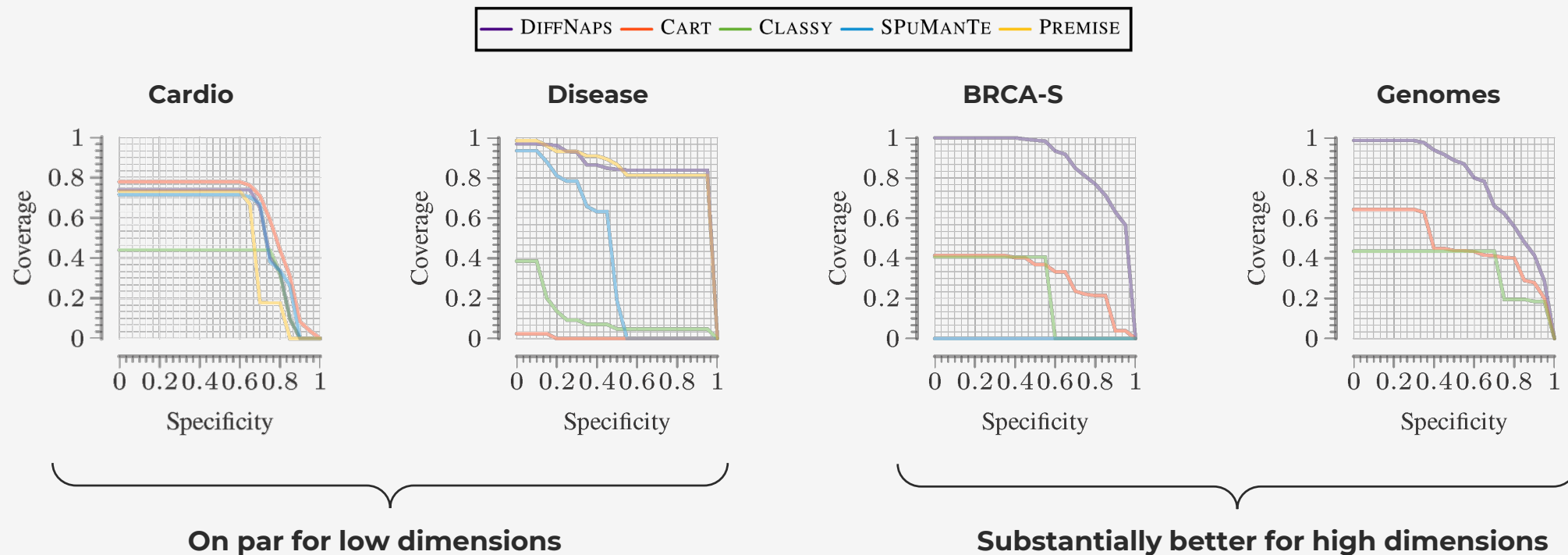
$$W_b^C = \begin{bmatrix} 0 & 0 & \mathbf{1} \\ 0 & \mathbf{1} & 0 \end{bmatrix}$$

Class-specific patterns: $P^1 = \{\{2,3\}\}$ resp. $P^2 = \{\{1,4\}\}$

DIFFNAPS – Real World Data



- **Cardio** ($m = 45$): Patient data annotated with heart disease
- **Disease** ($m = 131$): Various symptoms annotated with disease
- **BRCA-S** ($m = 20k$): ncRNA annotated with cancer type → Found biologically **relevant** patterns!
- **Genomes** ($m = 225k$): DNA annotated with ethnicity



Common questions in ML



Common questions in ML

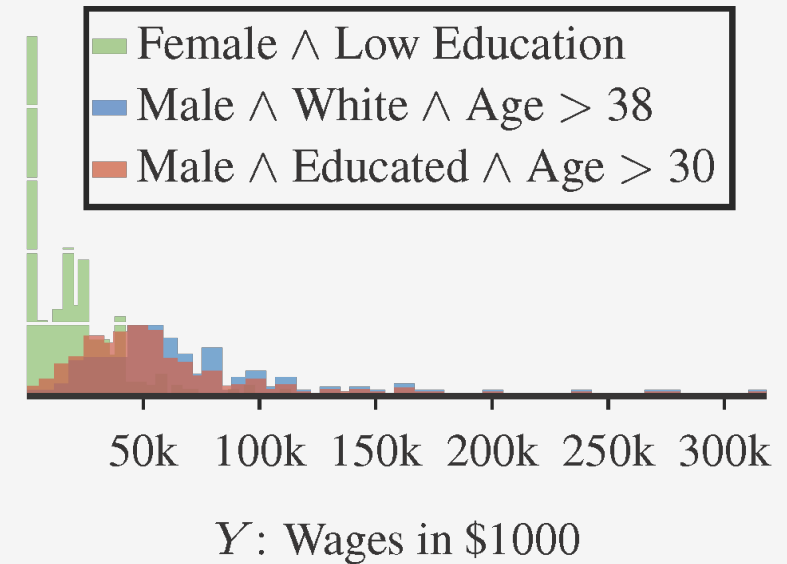


Discovering exceptional subgroups



Census Data

Sex	Height	Ethn	Education	Age	Income
♀	168	White	12	72	17k
♂	163	White	11	55	23k
♀	160	White	5	62	1k
♂	188	White	16	38	63k
♀	165	White	9	45	4k
♂	172	White	12	78	71k
♀	180	White	8	74	1k



Task – Subgroup Discovery:

1. Find **exceptional** subgroups
2. With an **interpretable** description

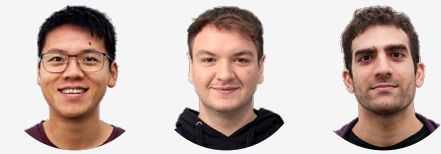
Traditional Subgroup Discovery



Subgroup Discovery

1. Pre-discretize features
→ **Likely to miss subgroups**
2. Strong assumptions on target
→ **Specialized methods needed**
3. Combinatorial optimization
→ **Does not scale**

Modern Subgroup Discovery



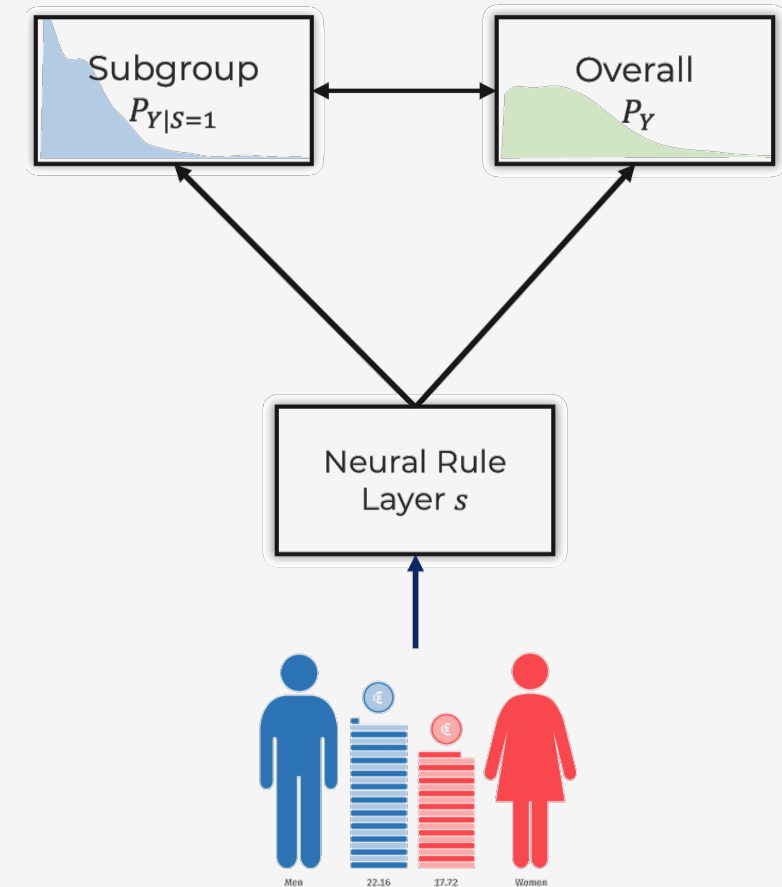
Subgroup Discovery

SYFLOW

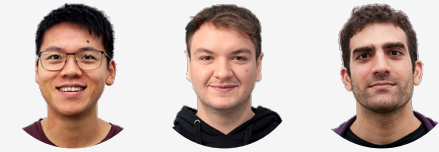
1. Pre-discretize features
→ **Likely to miss subgroups**
2. Strong assumptions on target
→ **Specialized methods needed**
3. Combinatorial optimization
→ **Does not scale**

1. Learn predicates end-to-end
→ **Accurate Discretization**
2. Use Normalizing Flows (NFs)
→ **No assumptions**
3. Maximize KL-divergence
→ **Highly general**
4. Continuous optimization
→ **Highly scalable**

$$\max KL(P_{Y|S=1} | P_Y)$$



SyFLOW – Neural Rule Layer I



Goal: Find an crisp interpretable description

$$\sigma(x) = \neg \text{Smoker} \wedge 44 < \text{Age} < 64$$

Ingredients:

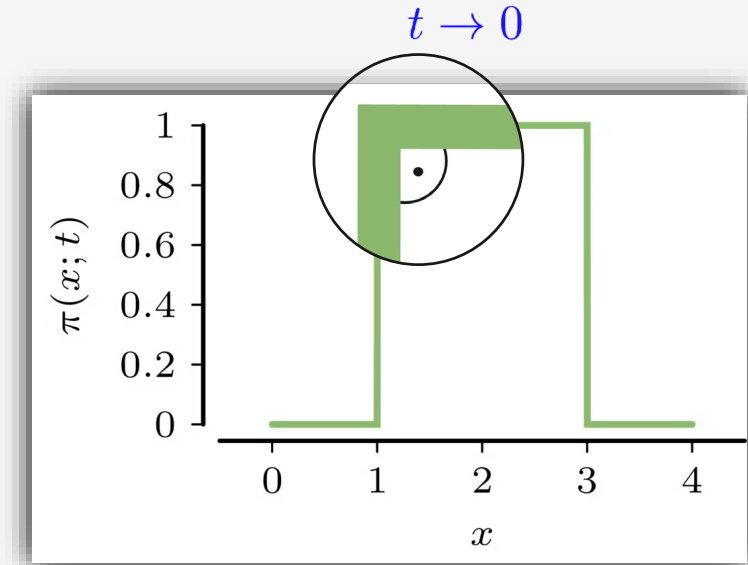
1. Differentiable binning predicate

$$\hat{\pi}(x_i; \alpha_i, \beta_i, t) = \frac{e^{\frac{1}{t}(2x_i - \alpha_i)}}{e^{\frac{1}{t}x_i} + e^{\frac{1}{t}(2x_i - \alpha_i)} + e^{\frac{1}{t}(3x_i - \alpha_i - \beta_i)}}$$

- Differentiable analog of:

$$\pi(x_i; \alpha_i, \beta_i) = \begin{cases} 1 & \text{if } \alpha_i < x_i < \beta_i \\ 0 & \text{otherwise} \end{cases}$$

- Temperature t controls crispness



Theorem 1 Given its lower and upper bounds $\alpha_i, \beta_i \in \mathbb{R}$, the soft predicate of Eq. (1) applied on $x \in \mathbb{R}$ converges to the crisp predicate that decides whether $x \in (\alpha, \beta)$,

$$\lim_{t \rightarrow 0} \hat{\pi}(x_i; \alpha_i, \beta_i, t) = \begin{cases} 1 & \text{if } \alpha_i < x_i < \beta_i \\ 0.5 & \text{if } x_i = \alpha_i \vee x_i = \beta_i \\ 0 & \text{otherwise} \end{cases}$$

SyFLOW – Neural Rule Layer II

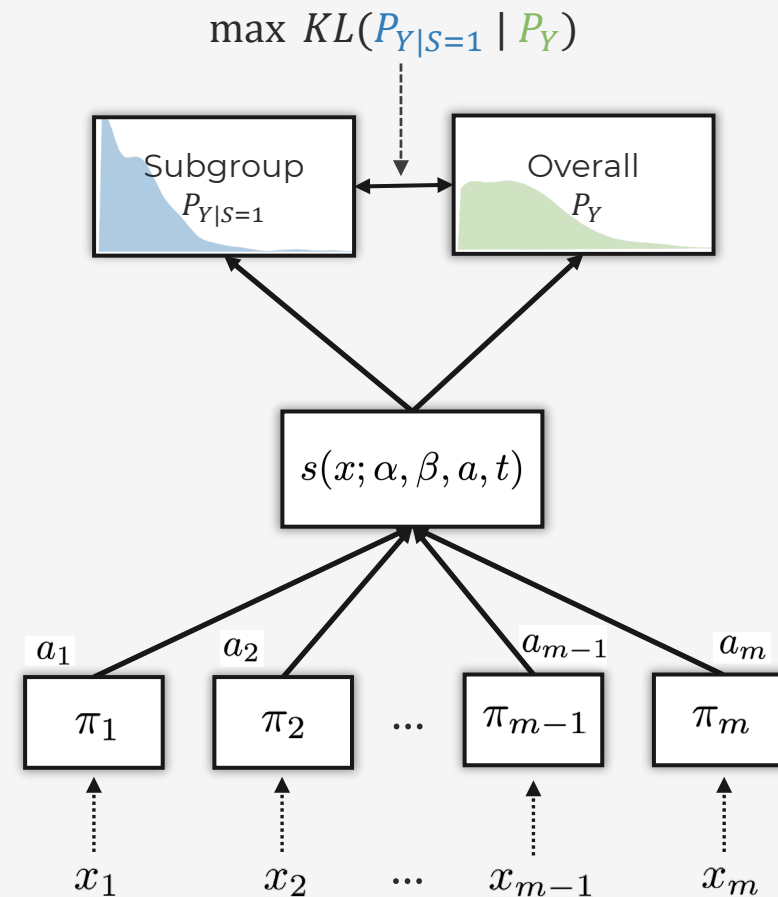


Ingredients:

1. Differentiable binning predicate
2. Differentiable logical *AND*
 - Harmonic means behaves like an *AND*
 1. If one π_i is zero then evaluate to false
 2. If all π_i are one then evaluate to true
 - Implicit feature selection with a_i

Optimization

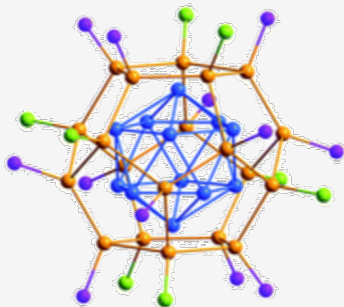
1. Learn the overall distribution P_Y
 2. Learn the subgroup distribution $P_{Y|S=1}$
 3. Optimize classifier weights and bins
 4. Output: Subgroup
- } Repeat for N steps



Fully differentiable!

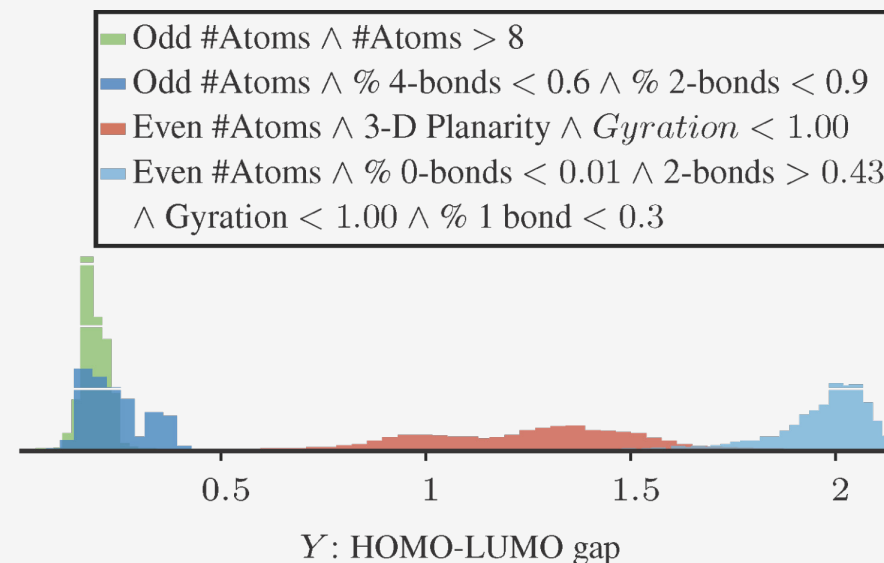


Gold Nanoclusters



- Atom-based features
- Bond-based features
- Shape-based features

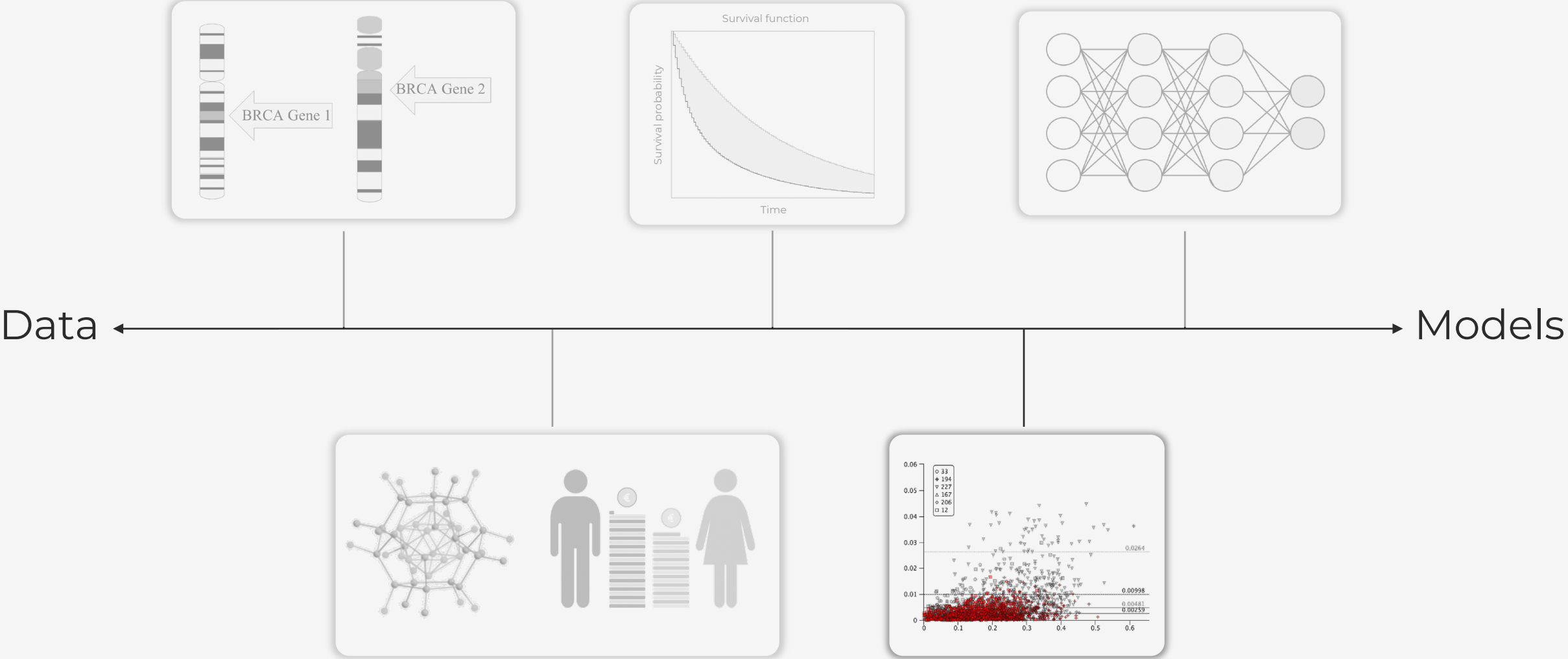
Target: HOMO-LUMO gap
~ stability and conductivity



Common questions in ML



Common questions in ML



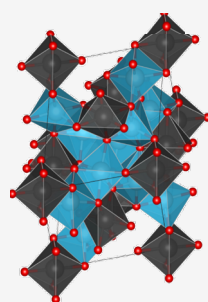
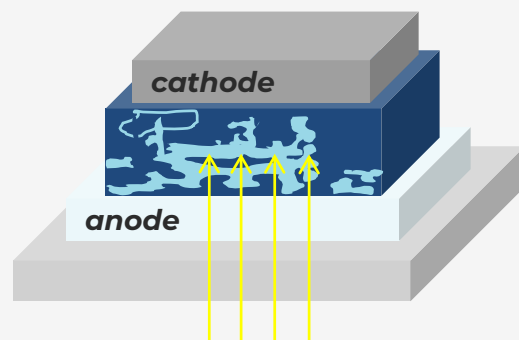
Model diagnostics



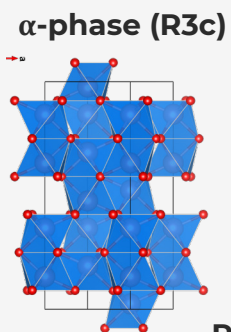
Population

$$P = \{c: c \in (\text{In}_x\text{Ga}_y\text{Al}_y)_2\text{O}_3\}$$

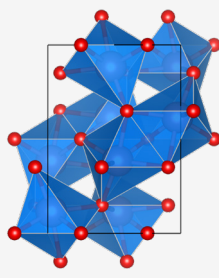
Photovoltaics



c-phase (Ia3)

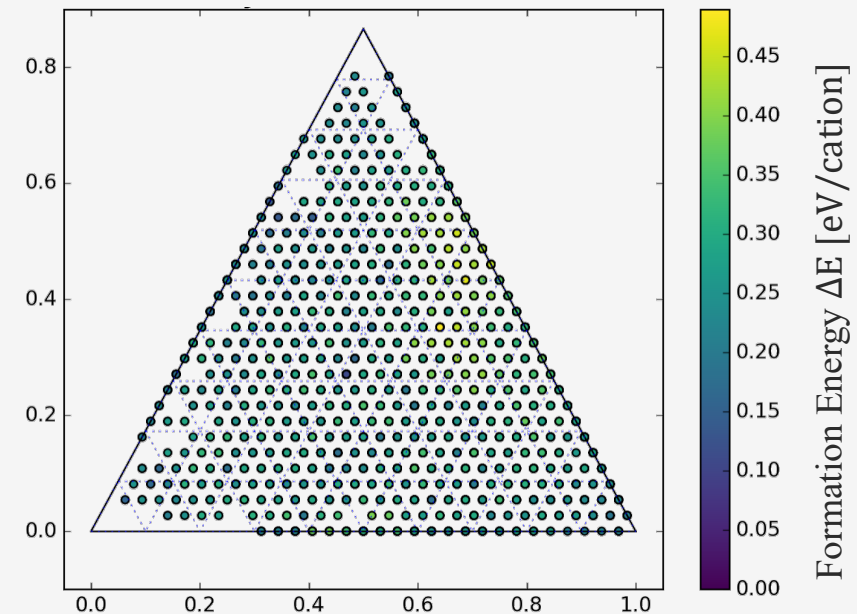
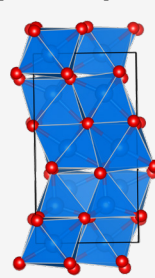


α -phase (R3c)



Rh_2O_3 -II-phase (Pbcn)

e-phase (Pna21)



Model diagnostics

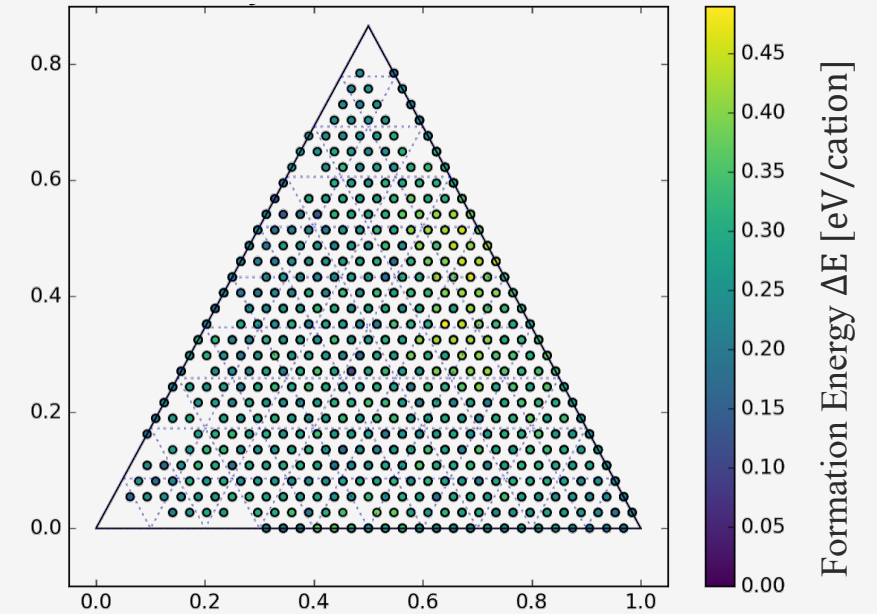
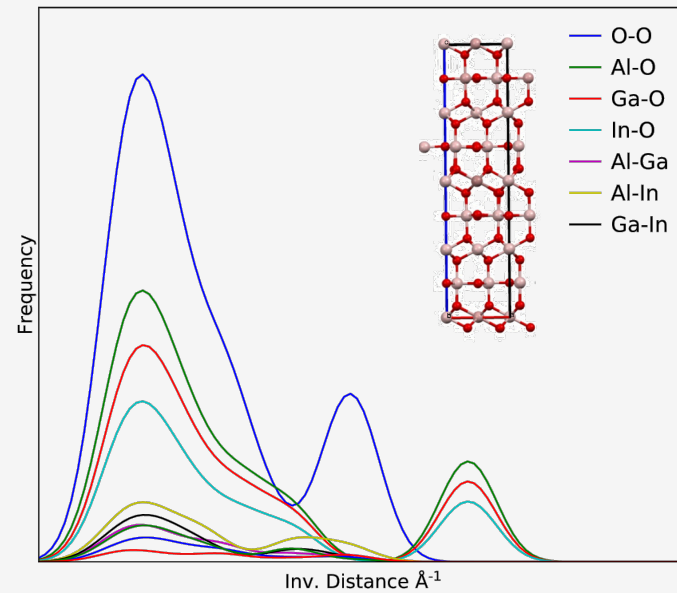


Population

$$P = \{c: c \in (\text{In}_x\text{Ga}_y\text{Al}_y)_2\text{O}_3\}$$

Target

$$y = |\Delta E - \tilde{f}_{\Delta E}(c)| \text{ of regression model } \tilde{f}_{\Delta E}$$



Arbitrary model you want
to use for predicting

Model diagnostics

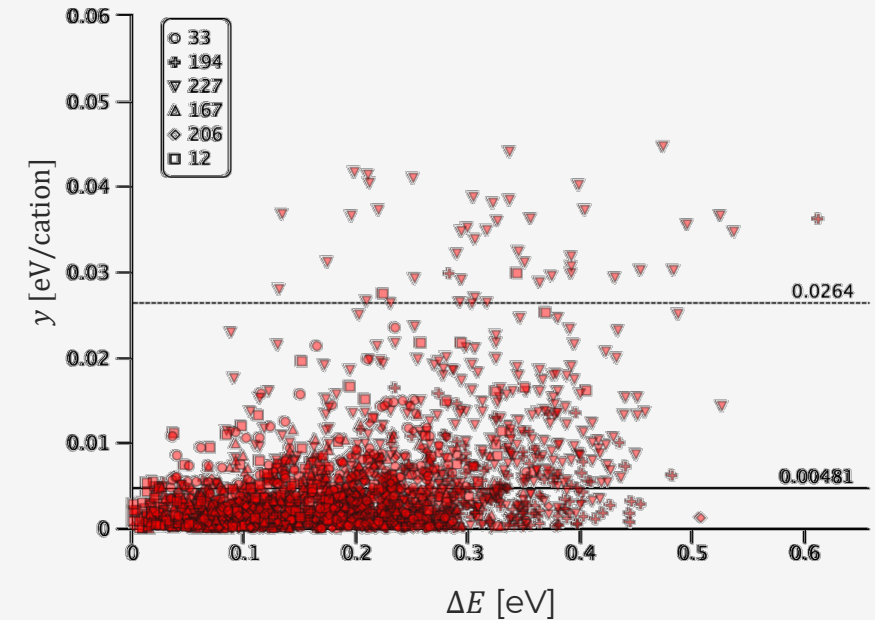
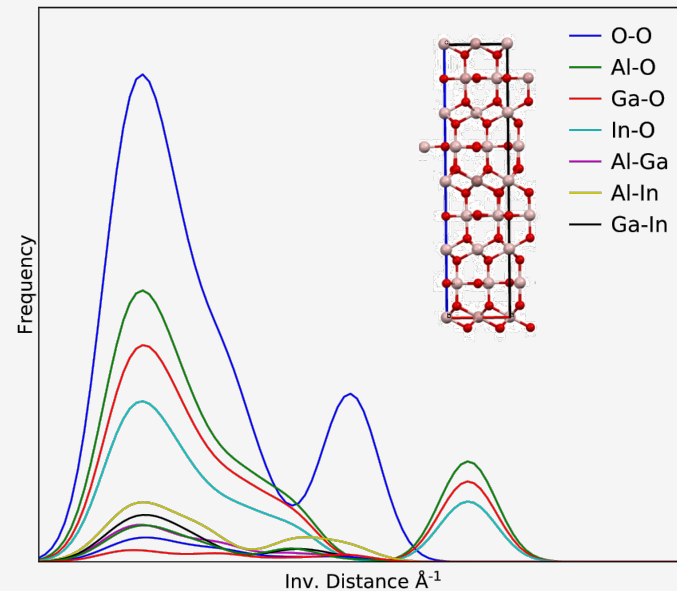


Population

$$P = \{c: c \in (\text{In}_x\text{Ga}_y\text{Al}_y)_2\text{O}_3\}$$

Target

$$y = |\Delta E - \tilde{f}_{\Delta E}(c)| \text{ of regression model } \tilde{f}_{\Delta E}$$



Model has low average error
but its predictions are
generally unreliable

Model diagnostics



Population

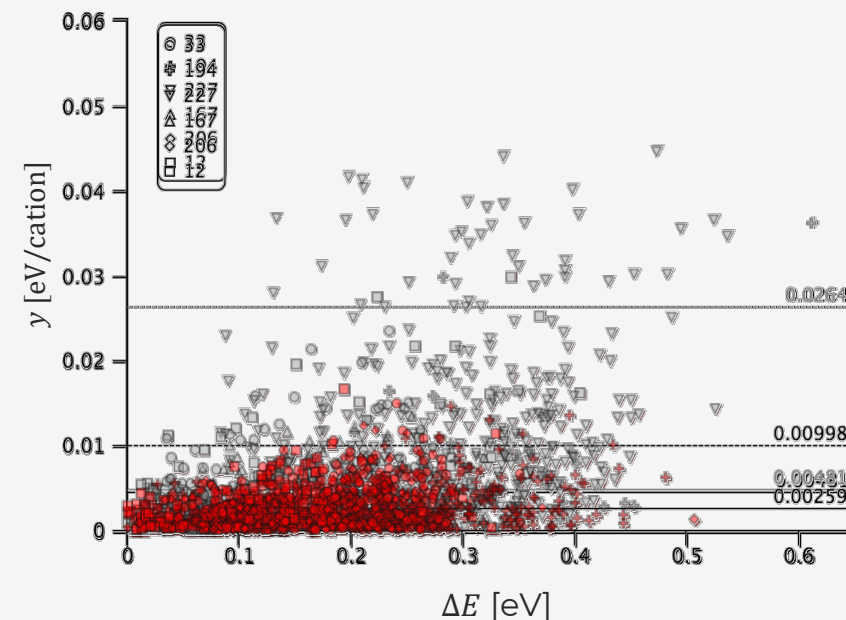
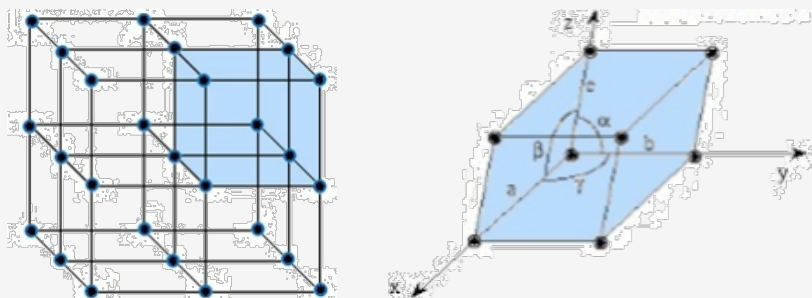
$$P = \{c: c \in (\text{In}_x\text{Ga}_y\text{Al}_y)_2\text{O}_3\}$$

Target

$$y = |\Delta E - \tilde{f}_{\Delta E}(c)| \text{ of regression model } \tilde{f}_{\Delta E}$$

Features

$$x \in \{a, b, c, \alpha, \beta, \gamma, n, \dots\}$$

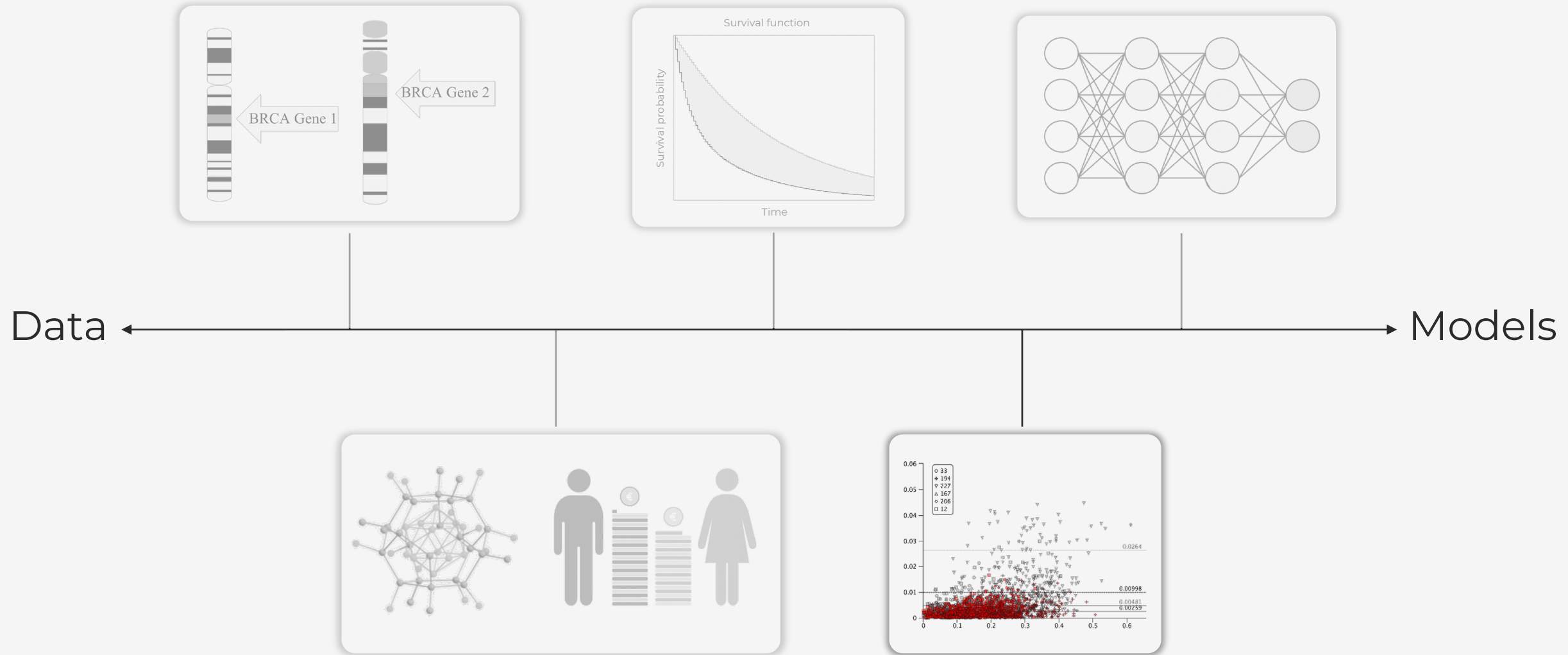


Model is **very reliable**
under these conditions

Selector $\sigma(c) \equiv n(c) \geq 60 \wedge \gamma(c) \leq 95 \wedge \alpha(c) \leq 121$

Parameters $\text{cvr}(\sigma) = 0.6$ $\text{eff}(\sigma) = 0.3$ $[\bar{y}(Q) = 0.003 \pm 0.002, \bar{y}(S) = 0.005 \pm 0.007]$

Common questions in ML

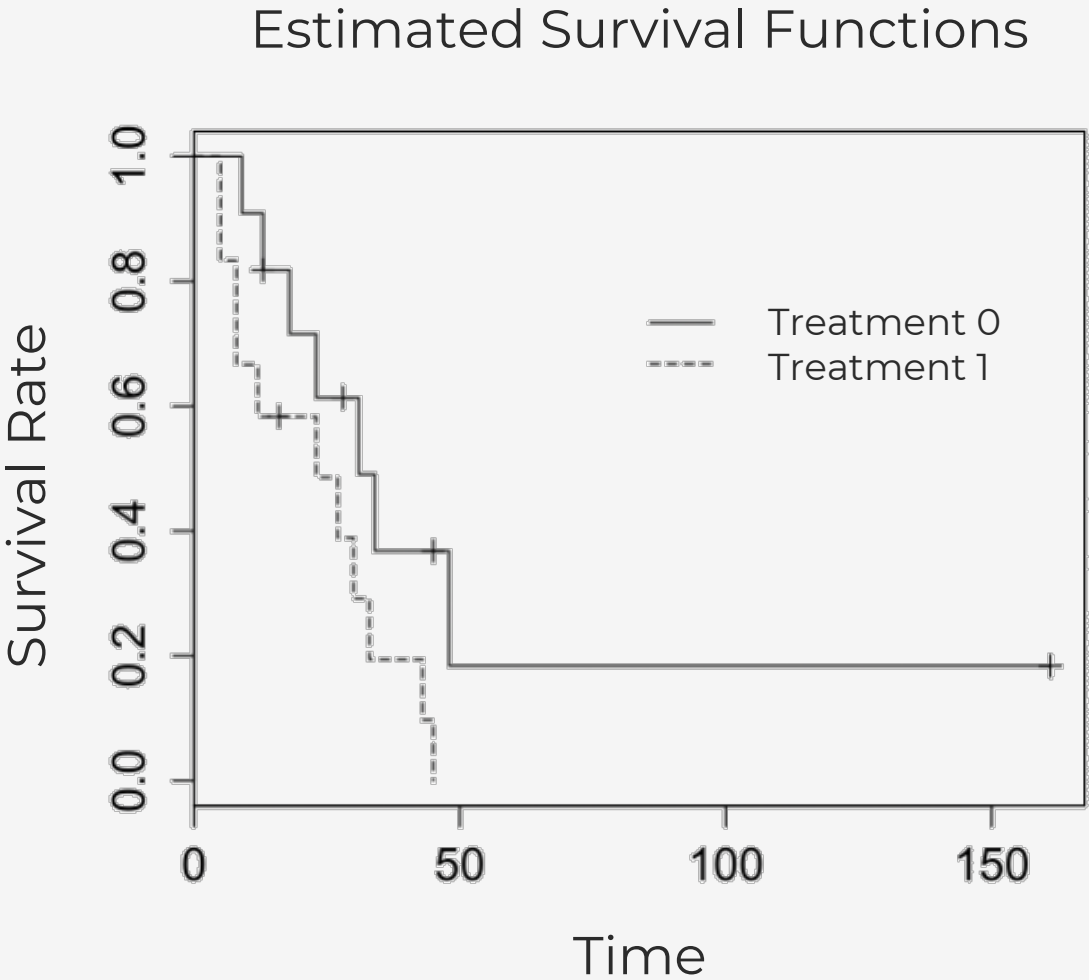


Common questions in ML



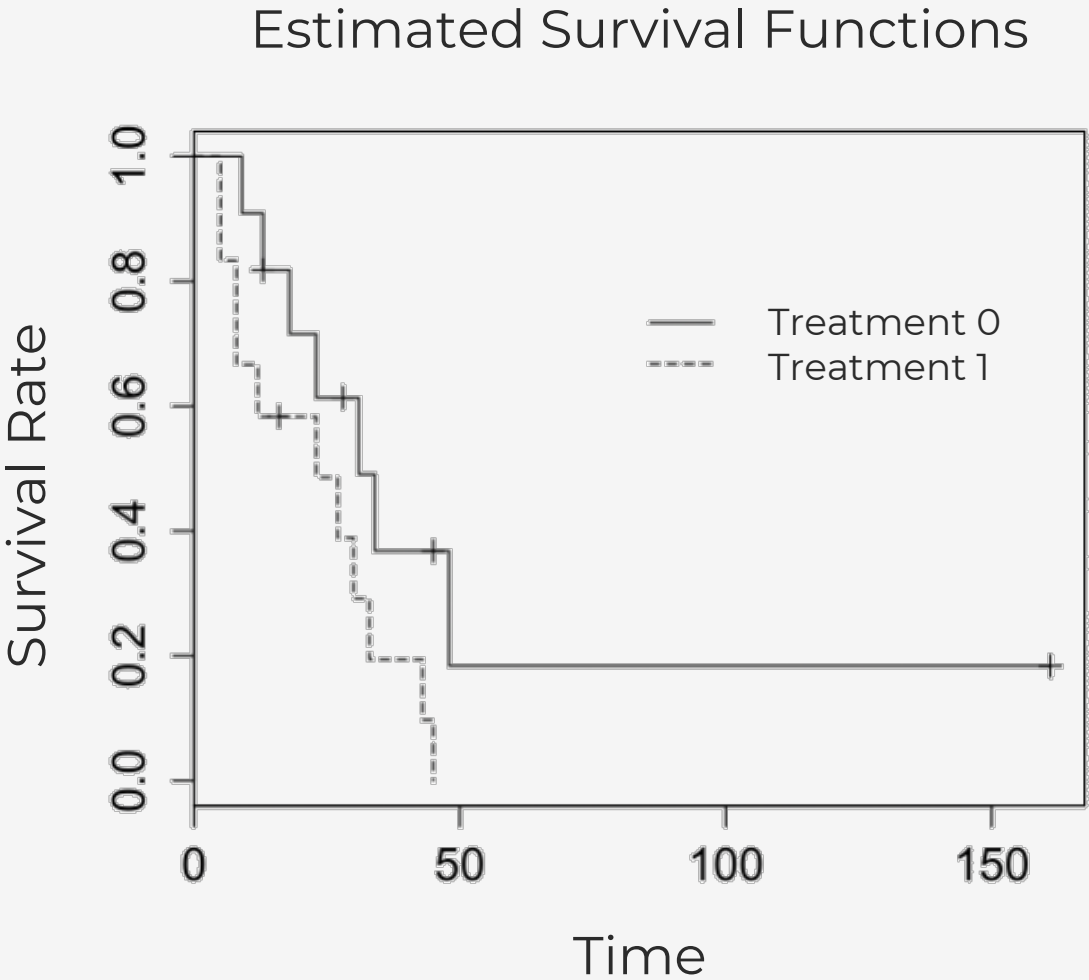
Time-to-event data

Participant	Treatment	Time of death
12	0	5
4	1	18
13	0	5
17	0	16
14	0	8
3	1	13
15	0	8
2	1	13
1	1	9
16	0	12



Time-to-event data

Participant	Treatment	Time of death
12	0	5
4	1	18
13	0	survived
17	0	left study
14	0	8
3	1	13
15	0	8
2	1	13
1	1	9
16	0	12



Survival Subgroups

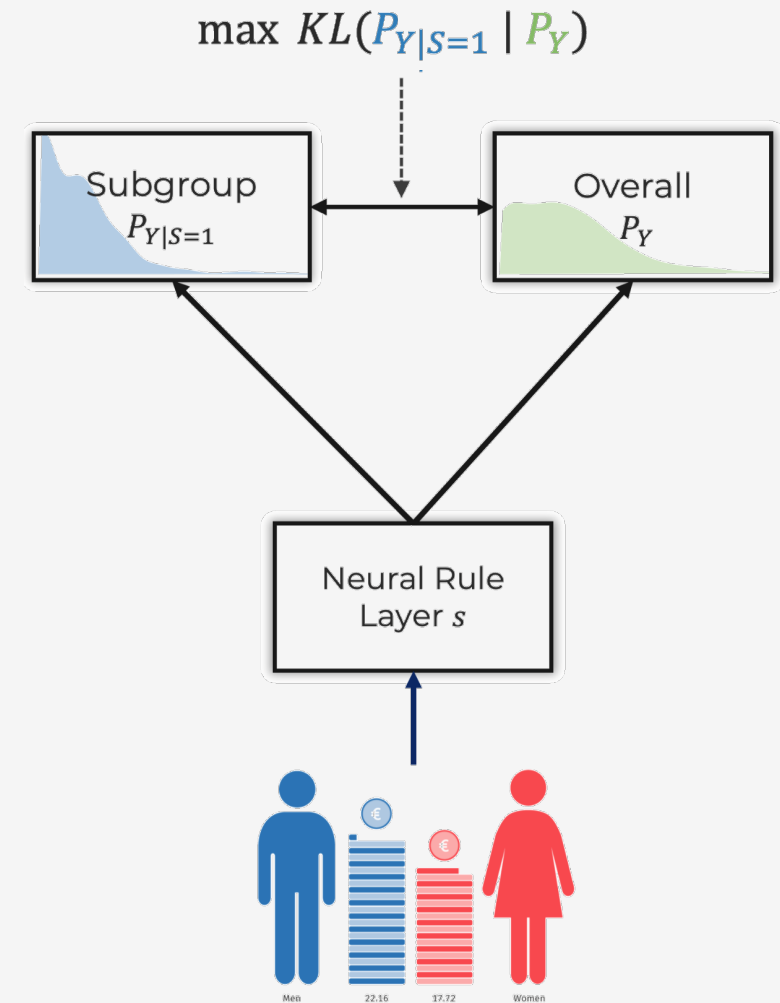


SYFLOW

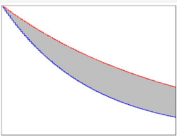
1. Learn predicates end-to-end
→ **Accurate Discretization**
2. Continuous optimization
→ **Highly scalable**
3. Use Normalizing Flows (NFs)
→ **Ignores censoring**

SYSURV

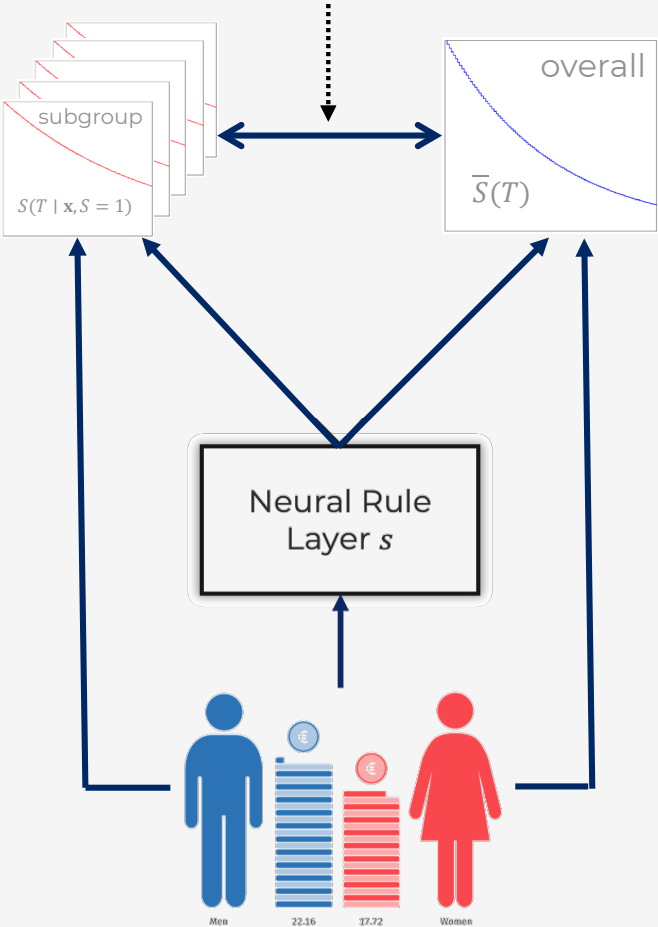
1. Learn predicates end-to-end
→ **Accurate Discretization**
2. Continuous optimization
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Survival Subgroups



$$\max_{\mathbf{f}} \max_{\mathbf{d}} \text{KL}(\bar{d}_1(\mathbf{x}) || P_Y)$$



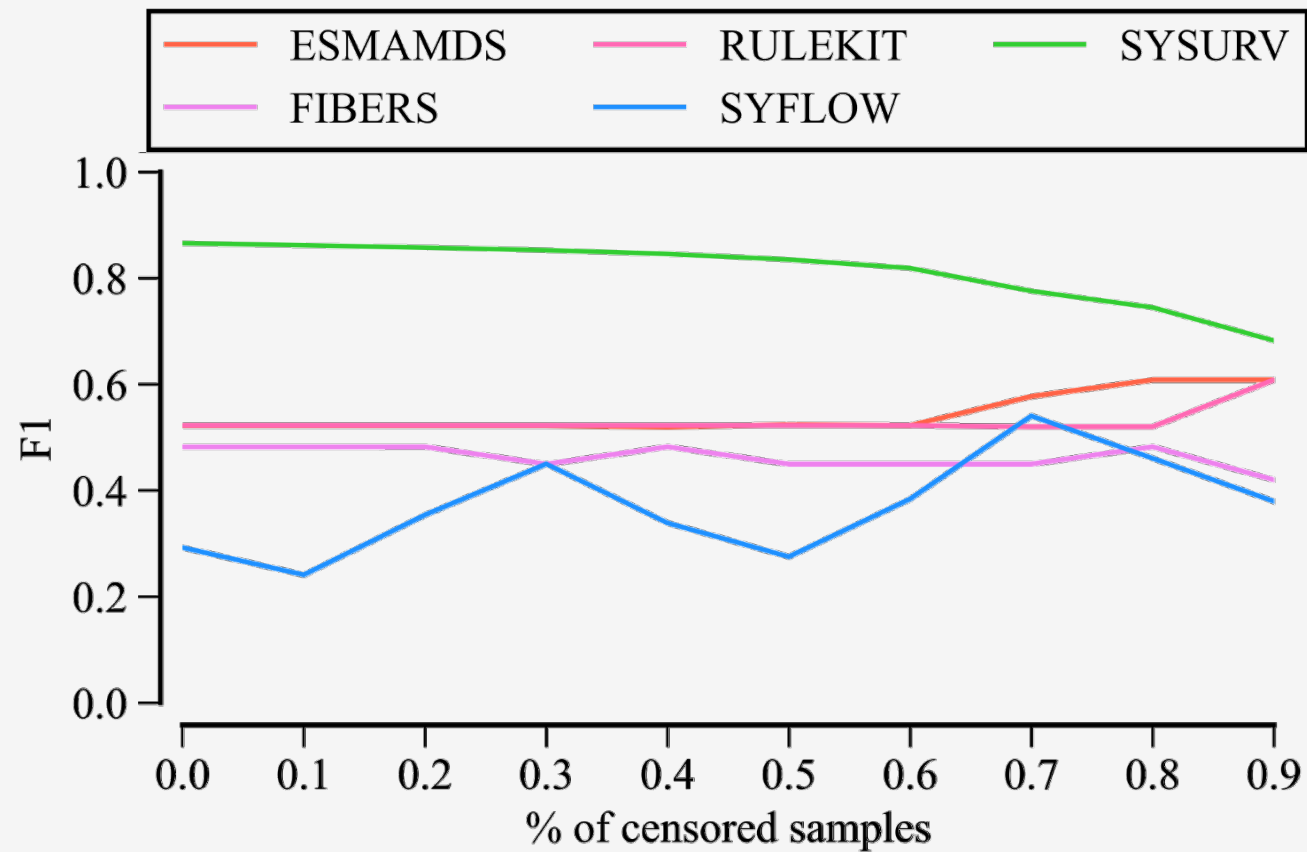
SYFLOW

SYSURV

- 1. Learn predicates end-to-end
→ **Accurate Discretization**
- 2. Continuous optimization
→ **Highly scalable**
- 3. Use Normalizing Flows (NFs)
→ **Ignores censoring**
- 4. Uses KL-Divergence
→ **Ignores survival**

- 1. Learn predicates end-to-end
→ **Accurate Discretization**
- 2. Continuous optimization
→ **Highly scalable**
- 3. Use Random Survival Forests
→ **No assumptions**
- 4. Maximize curve distance
→ **No assumptions**

Experiments — Synthetic data



Experiments — Real world

	Our objective					KL-Divergence					Logrank statistic					Mean-shift					Adjusted mean-shift				
	SYSURV	SYFLOW	ESMAMDS	FIBERS	RULEKIT	SYSURV	SYFLOW	ESMAMDS	FIBERS	RULEKIT	SYSURV	SYFLOW	ESMAMDS	FIBERS	RULEKIT	SYSURV	SYFLOW	ESMAMDS	FIBERS	RULEKIT	SYSURV	SYFLOW	ESMAMDS	FIBERS	RULEKIT
UnempDur	6.37	3.20	3.79	3.79	3.79	0.08	0.15	0.13	0.13	0.13	19.26	125.99	125.00	125.00	226.52	-2.01	-1.74	2.14	2.14	2.14	-0.02	-0.00	0.00	0.00	0.00
nwtco	1011.64	205.02	680.98	208.59	680.98	0.14	0.02	0.06	0.00	0.06	374.22	0.21	31.36	0.00	281.27	1161.97	872.08	688.24	-0.56	688.24	6.92	0.40	1.50	-0.00	1.50
rott2	559.22	419.19	487.58	487.58	326.16	-	-	-	-	-	266.95	3.11	71.65	169.35	93.04	31.47	-92.00	25.23	25.23	10.03	0.10	-11.50	0.04	0.04	0.01
rdata	259.24	153.69	213.83	158.52	213.83	0.08	0.04	0.03	0.01	0.03	113.38	56.39	14.64	43.32	107.75	1116.58	-700.91	933.49	705.50	933.49	7.98	-1.72	3.60	1.62	3.60
Aids2	66.64	31.99	54.01	34.69	60.52	-	-	-	-	-	0.21	0.00	4.27	0.01	1.72	22.68	-1.45	61.36	-0.70	61.21	0.07	-0.00	0.10	-0.00	0.17
Dialysis	4.52	4.69	4.71	4.59	4.74	0.02	0.24	0.01	0.02	0.04	6.36	33.76	70.86	305.94	68.38	0.64	-19.60	3.05	4.47	5.74	0.00	-0.19	0.00	0.00	0.02
TRACE	261.76	486.65	332.10	261.58	272.52	0.00	-	0.02	4.98	0.01	0.00	17.74	93.24	0.00	94.62	0.00	4.53	1.73	-0.00	0.61	0.00	4.53	0.00	-0.00	0.00
support2	132.83	68.72	104.90	54.79	81.38	2.71	0.57	1.36	0.22	0.21	251.00	39.00	46.83	11.93	59.87	405.72	-193.91	405.52	-71.03	227.60	12.29	-1.41	5.13	-0.16	2.35
dataDIVAT2	286.30	99.92	172.47	141.30	141.30	0.16	3.91	1.41	2.19	2.19	33.55	15.90	10.94	31.60	31.60	3.18	-1.06	2.06	1.56	1.56	0.05	-0.00	0.01	0.00	0.00
prostateSurvival	20.11	9.20	14.13	5.38	7.51	-	-	-	-	-	425.72	103.66	82.50	82.50	64.74	6.11	5.11	3.37	-1.02	3.67	0.00	0.00	0.00	-0.00	0.00
actg	34.58	13.62	18.82	11.33	24.22	0.09	0.03	0.03	0.00	0.06	59.97	2.40	12.26	0.02	1.05	54.13	18.50	5.98	-0.37	27.30	1.42	0.07	0.03	-0.00	0.22
scania	172.47	101.59	147.42	84.74	147.42	0.03	0.00	0.03	0.01	0.03	4.65	1.91	13.66	9.93	14.66	6.51	-2.86	-2.44	-0.07	-2.44	0.05	-0.00	-0.01	-0.00	-0.01
grace	38.56	32.04	21.01	13.08	16.51	0.14	0.06	7.53	0.02	0.00	59.30	70.71	28.68	13.81	33.33	64.03	51.79	21.77	-11.14	16.00	1.94	0.54	0.08	-0.02	0.04
Avg. rank	1.54	3.85	2.46	4.23	2.92	2.50	2.67	2.80	3.75	3.05	2.38	3.46	3.08	3.65	2.42	2.08	2.85	2.85	4.23	3.00					

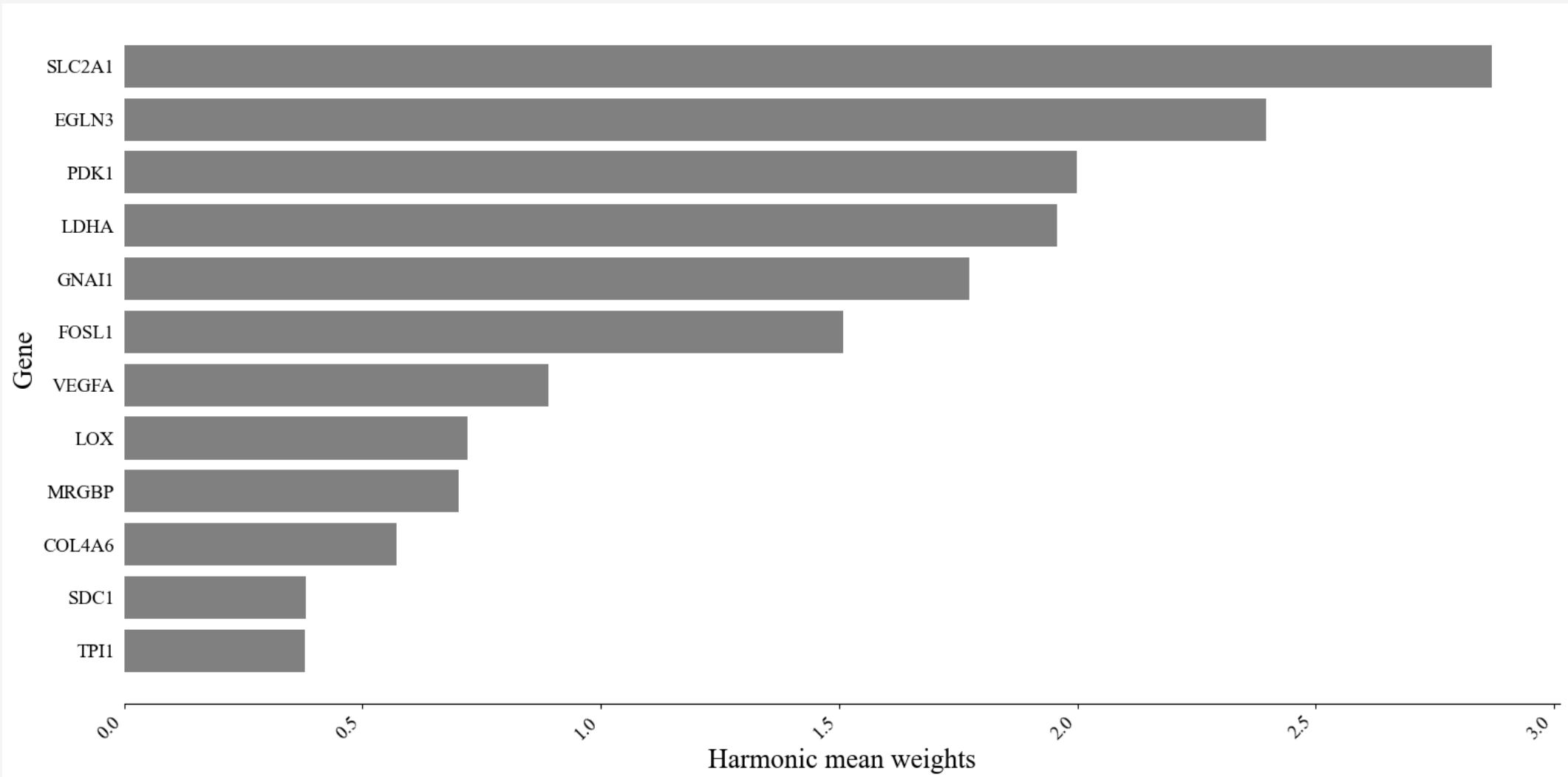
Experiments — Real world

<i>Avg. Rank</i>	SYSURV	SYFLOW	ESMAMDS	FIBERS	RULEKIT
Our objective	1.54	3.85	2.46	4.23	2.92
KL-Divergence	2.50	2.67	2.80	3.75	3.05
Logrank statistic	2.38	3.46	3.08	3.65	2.42
Mean-shift	2.08	2.85	2.85	4.23	3.00

Case Study: Neck Carcioma



PCR - first rule (pruned) -> All associated with Hypoxia



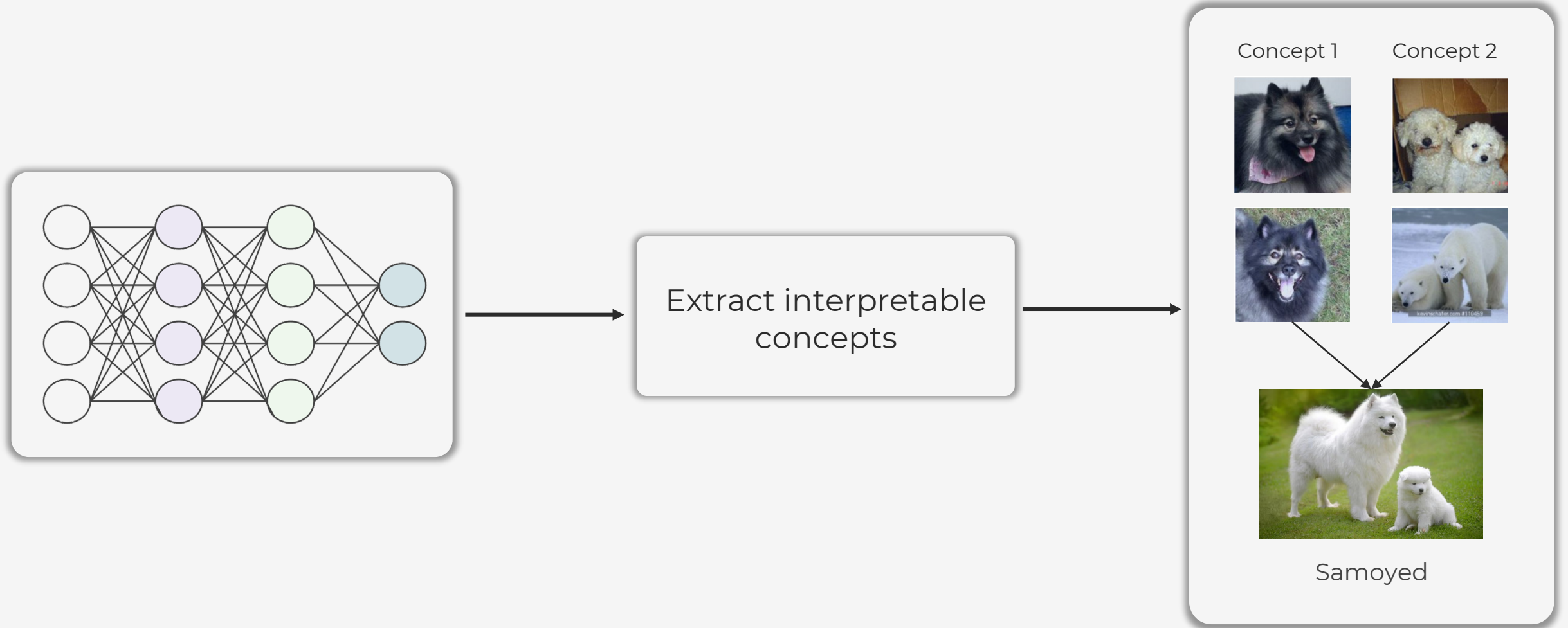
Common questions in ML



Common questions in ML



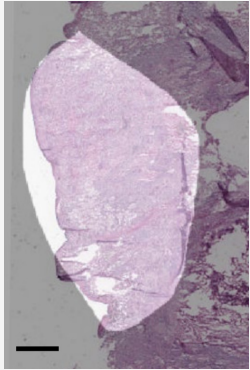
Understanding reasoning



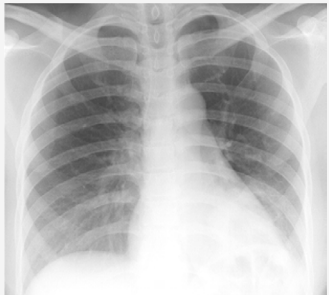
Why is it important?



Gaining new scientific insights



“... 45 out of 54 of the TCGA images **misclassified by at least one of the pathologists** were **assigned** to the **correct** cancer type **by the algorithm**”.



COVID-Net

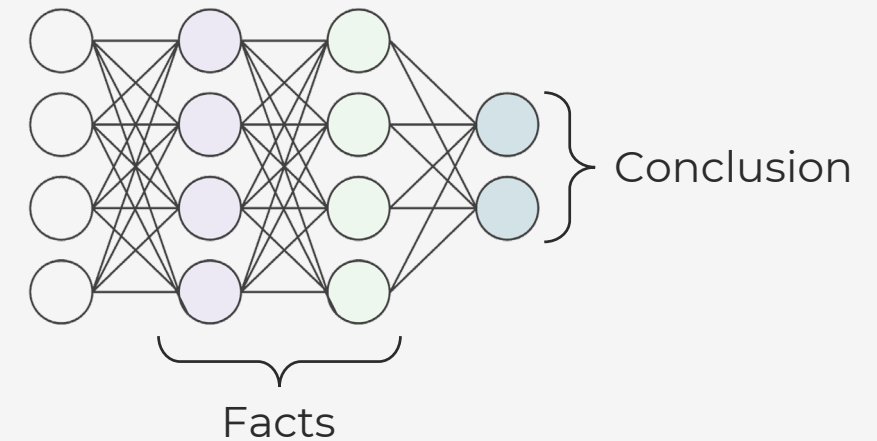
Gain insights into **critical factors** associated with **COVID** cases

What is **reasoning**?

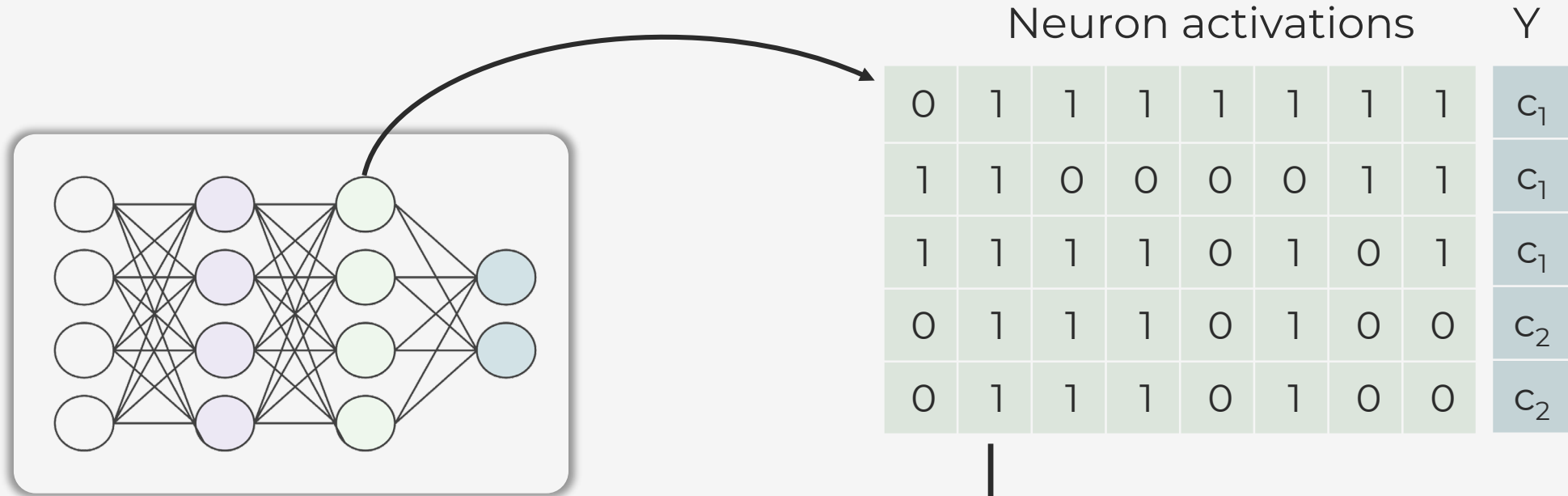
„Reasoning is the process by which you reach a **conclusion** after thinking about all the **facts**.“

— Collins dictionary

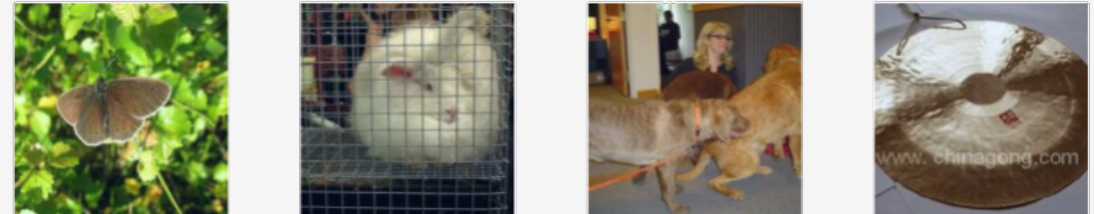
i.e. a relation between **facts** and a **conclusion**



Extracting Features



Neurons are polysemantic



Sneak peek – Information Flow

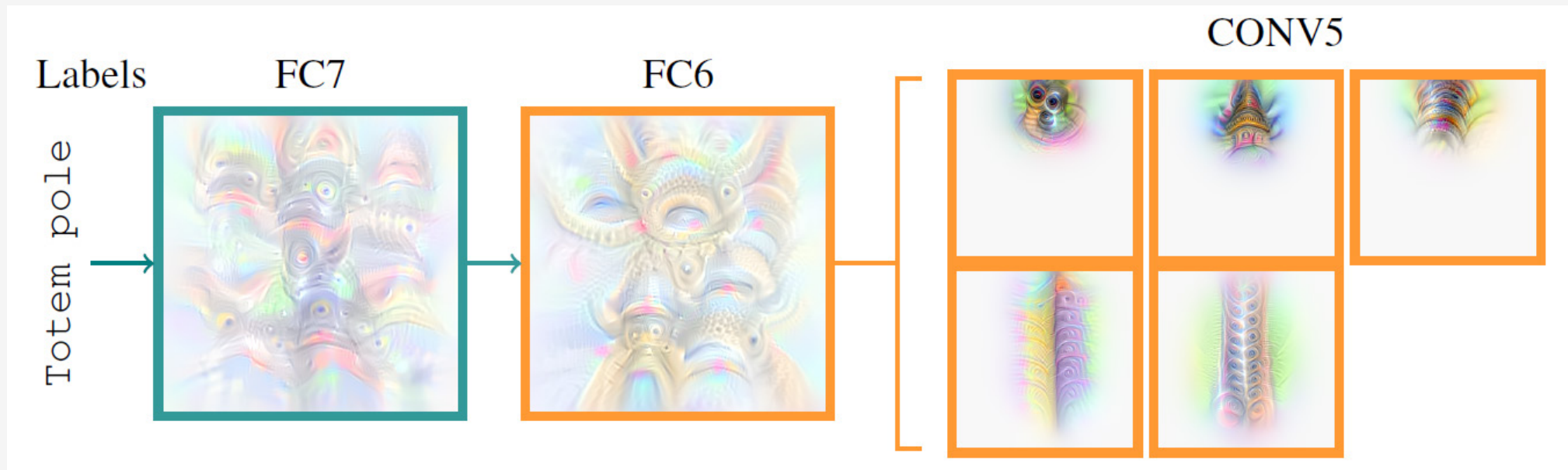


How does information flow and how is it combined?

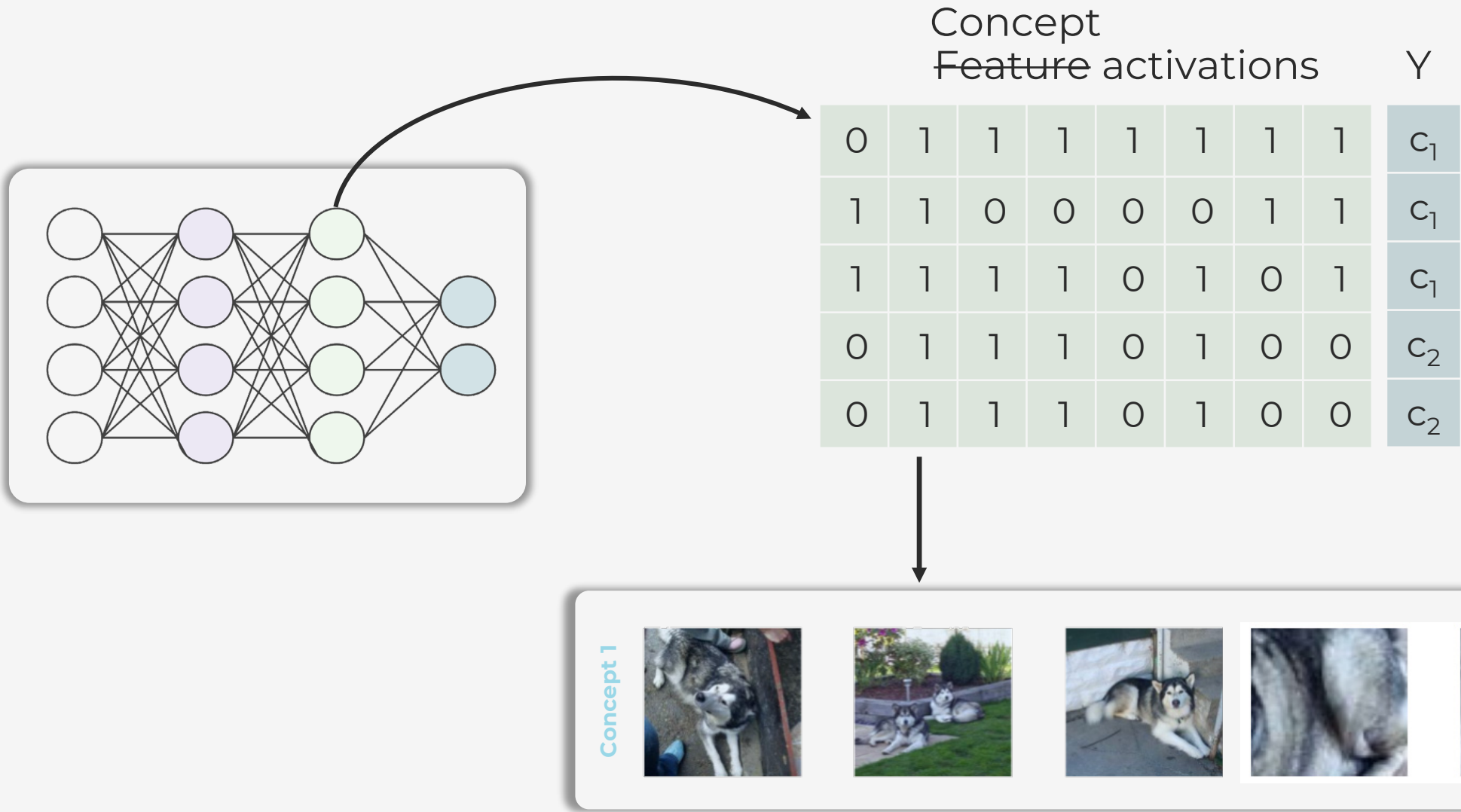
Rules: $X \rightarrow Y,$ $X \in \text{Labels}, Y \in \text{FC7}$

$Y \rightarrow Z,$ $Z \in \text{FC6}$

$Z \rightarrow Q,$ $Q \in \text{CONV5}$



Extracting Features Concepts



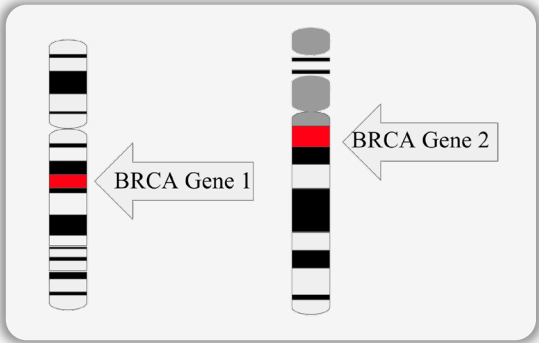
Connecting concepts



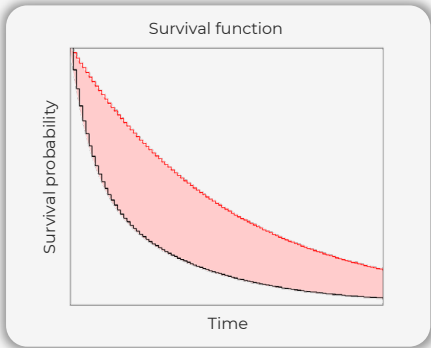
Conclusion



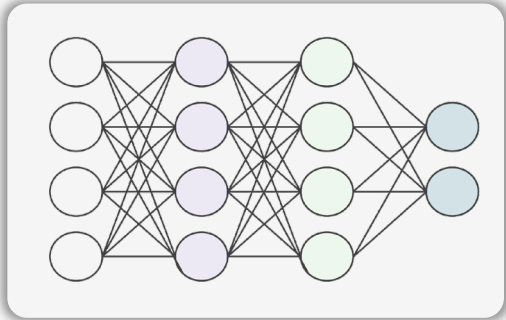
DIFFNAPS



SYSURV

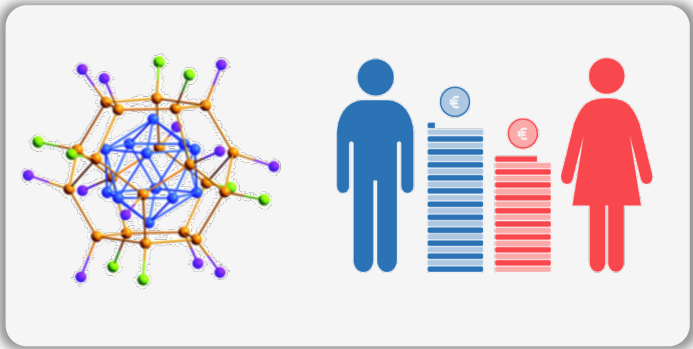


EXPLAINNAPS

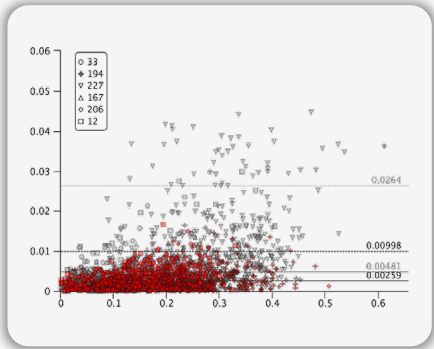


Data

Models



SYFLOW



DOMAINS OF APPLICABILITY